



Ref. No.:

Date: 15- May, 2020

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CORE CONCEPT OF

BUSINESS MATHEMATICS & STATISTICS

1. Illustrate the Index Number.
2. Briefly describe the characteristics of index number.
3. What do you mean by purpose of index number?

Example-20: Compute Laspeyre's, Paasche's, Marshall-Edge worth's, Dorbish Bowley's, Fisher's Ideal Index Number. Also satisfy the test from the following data:

Items	Base Year		Current Year	
	Price	Expenditure (value)	Price	Expenditure(value)
A	10	100	12	144
B	15	75	20	120
C	8	80	10	110
D	20	60	25	50
E	50	500	60	540

Solution-20:

Items	Base Year		Current Year		q0	q1	P0q0	P0q1	P1q0	P1q1
	p0	(value)	p1	(value)						
A	10	100	12	144	10	12	100	120	120	144
B	15	75	20	120	5	6	75	90	100	120
C	8	80	10	110	10	11	80	88	100	110
D	20	60	25	50	3	2	60	40	75	50
E	50	500	60	540	10	9	500	450	600	540
							ΣP0q0 815	ΣP0q1 788	Σp1q0 995	Σp1q1 964

1) Laspeyre's Method: $(P_{01}) = \left[\frac{\sum P_1 q_0}{\sum P_0 q_0} * 100 \right]$



$$(P_{01}) = \left[\frac{995}{815} * 100 \right] = 1.221 * 100 = 122.09$$

2) Paasche's Method: $(P_{01}) = \left[\frac{\sum P_1 q_1}{\sum P_0 q_1} * 100 \right]$

$$(P_{01}) = \left[\frac{964}{788} * 100 \right] = 1.2234 * 100 = 122.34$$

3) Marshall-Edge worth's Method: $(P_{01}) = \left[\frac{\sum P_1 q_0 + \sum P_1 q_1}{\sum P_0 q_0 + \sum P_0 q_1} * 100 \right]$

$$(P_{01}) = \left[\frac{995 + 964}{815 + 788} * 100 \right]$$

$$(P_{01}) = \left[\frac{1959}{1603} * 100 \right] = 1.222 * 100 = 122.2$$

4) Dorbish Bowley's Method- $(P_{01}) = \left[\frac{\sum P_1 q_0}{\sum P_0 q_0} + \frac{\sum P_1 q_1}{\sum P_0 q_1} \right] * 100 / 2$

$$(P_{01}) = \left[\frac{995}{815} + \frac{964}{788} \right] * 50$$

$$(P_{01}) = [1.221 + 1.223] * 50$$

$$(P_{01}) = [2.444] * 50 = 122.2$$

5) Fisher's Index Number = $(P_{01}) = \sqrt{\frac{\sum P_1 q_0}{\sum P_0 q_0} * \frac{\sum P_1 q_1}{\sum P_0 q_1}} * 100$

$$(P_{01}) = \sqrt{\frac{995}{815} * \frac{964}{788}} * 100$$

$$(P_{01}) = \sqrt{1.221 * 1.223} * 100$$

$$(P_{01}) = \sqrt{1.493283} * 100$$

$$(P_{01}) = 1.22 * 100 = 122$$



Reversibility Tests-

1) Time Reversibility test.

$$P_{01} * P_{10} = 1$$

Fisher's ideal index number satisfies this test as explained below:

$$(P_{01}) = \sqrt{\frac{\Sigma P_{1q0}}{\Sigma P_{0q0}} * \frac{\Sigma P_{1q1}}{\Sigma P_{0q1}}} * 100 \quad \text{or} \quad (P_{10}) = \sqrt{\frac{\Sigma P_{0q0}}{\Sigma P_{1q0}} * \frac{\Sigma P_{0q1}}{\Sigma P_{1q1}}} * 100$$

$$\text{Thus, } P_{01} \times P_{10} = \sqrt{\frac{\Sigma P_{1q0}}{\Sigma P_{0q0}} * \frac{\Sigma P_{1q1}}{\Sigma P_{0q1}} * \frac{\Sigma P_{0q0}}{\Sigma P_{1q0}} * \frac{\Sigma P_{0q1}}{\Sigma P_{1q1}}}$$

$$P_{01} \times P_{10} = \sqrt{\frac{995}{815} * \frac{964}{788} * \frac{815}{995} * \frac{788}{964}} = \sqrt{1}$$

$$P_{01} \times P_{10} = 1$$

2) Factor Reversibility Test- $P_{01} * Q_{01} = \frac{\Sigma P_{1q1}}{\Sigma P_{0q0}}$

Fisher's formula satisfies also this test as explained below:

$$(P_{01}) = \sqrt{\frac{\Sigma P_{1q0}}{\Sigma P_{0q0}} * \frac{\Sigma P_{1q1}}{\Sigma P_{0q1}}} * 100 \quad Q_{01} = \sqrt{\frac{\Sigma q_{1p0}}{\Sigma q_{0p0}} * \frac{\Sigma q_{1p1}}{\Sigma q_{0p1}}} * 100$$

$$P_{01} * Q_{01} = \sqrt{\frac{\Sigma P_{1q0}}{\Sigma P_{0q0}} * \frac{\Sigma P_{1q1}}{\Sigma P_{0q1}} * \frac{\Sigma q_{1p0}}{\Sigma q_{0p0}} * \frac{\Sigma q_{1p1}}{\Sigma q_{0p1}}}$$

$$P_{01} * Q_{01} = \sqrt{\frac{995}{815} * \frac{964}{788} * \frac{788}{815} * \frac{964}{995}}$$

$$P_{01} * Q_{01} = \sqrt{\frac{964}{815} * \frac{964}{815}}$$

$$P_{01} * Q_{01} = \frac{964}{815} = 1.183$$